## Basic Exercises on CafeOBJ

- basic commands, parsing, debugging, tracing, modeling, specification -


## CafeOBJ Team of JAIST

## Topics

- Basic commands of CafeOBJ system
- Inputting specifications, parsing, debugging, tracing
- A simple example of modeling and specification: STACK


## How to get CafeOBJ System

- Source code (in CommonLisp) and binary code for UNIX/Linus, MacOS, and Windows are available
- URL of CafeOBJ official home page: http://www.ldl.jaist.ac.jp/cafeobj/


Several Kinds of CafeOBJ Systems


## Starting System

- CafeOBJ system is invoked by typing "cafeobj" (or clicking CafeOBJ.bat or CafeOBJ.exe files), and the system waits for your input with a "prompt".

"Prompt" from CafeOBJ system shows the current module


## Quitting System

- By typing "quite" or "q" (or typing control-D; this depends on the OS you are using), you can quite from the CafeOBJ system

```
CafeOBJ> quit
[Leaving Cafe0BJ]
%
```

Inputting moudles or selecting modules

- In the top level of CafeOBJ system, the commands for inputting modules and selecting modules are available.

| Cafeobj> mod TEST \{[Elt ] \} | input |
| :--- | ---: |
| -- defining module TEST_* done. <br> CafeOBJ> | output |

After a inputting module, the module is available by typing "selecting <the module name>"

CafeOBJ> select TEST
TEST>
After selecting the module "ModName", the prompt is changed to "ModName>".

## System Error - error should be eliminated -

- warning needs not be eliminated, but recommended to be eliminated -
- CafeOBJ system report an error as follows:

CafeOBJ> mod ERROR \}
[Error]: was expecting the symbol `\{' not `\}' Cafe0bj>

- "[Error]..." reports a serious error like syntax error in inputted CafeOBJ code. CafeOBJ system may go down to CHAOS level for some special errors.

```
Cafe0BJ> ^C
Error: Received signal number 2 ...
[1c] CHAOS(1):
```

- From "CHAOS" level, CafeOBJ system will be recovered by typing ":q" in almost all cases.

```
[1c] CHAOS(1): :q
Cafe0BJ>
```


## Inputting files

- It is always recommended that CafeOBJ codes is prepared in some file and the file is inputted into CafeOBJ system by typing "in <fileName>" or "input <fileName>". The file extension of CafeOBJ file is ".mod".
example: inputting "test.mod" file

```
% more test.mod
    mod TEST { [Elt] }
    select TEST
%
CafeOBJ> in test.mod
processing input : /.../test.mod
-- defining module TEST._* done.
TEST>
```


## ?, show, describe, show ? commands

- By typing "?", you can see the list of commands which are available at the level.
- "show" command shows varieties of information
. "show <module name>", "show sorts", "show ops"
. "show ?" gives you a list of show commands available
. "show" can be shortened into "sh"

```
Cafe0BJ> ?
-- CafeOBJ top level commands :
-- Top level definitional forms include `module'(object, theory),
-- 'view', and 'make'
? print out this help
quit -or-
q exit from Cafe0BJ interpreter
select <Modexp> set the <Modexp> current
show -or- print various info., for further help, type 'show ?'
...
```


## set, set ? and show switches command

set command set switches of CafeOBJ system. By changing switches you can customize CafeOBJ system get different behaviors of the system.

```
CafeOBJ> set auto context on making system select the last
CafeOBJ> mod TEST { [ Elt] } entered module automatically
-- defining module TEST._* done.
TEST>
TEST> set ? Shows all set commands
TEST> ...
TEST> show switches
```


## Comments

A line beginning with "- " (or "**") is ignored, and A line beginning with "-->" (or "**>") is echoed back.

```
CafeOBJ> -- this is a comment
Cafe0BJ>
```

Cafeobj> --> this is a comment --> this is a comment Cafe0BJ>

CafeobJ> ** this is a comment Cafe0BJ>

CafeOBJ> **> this is a comment **> this is a comment Cafe0BJ>

It is very important to write as much appropriate comments as possible for explaining specifications and verifications/proofs.

```
...> select NAT+
NAT+> parse s 0 + 0.
((s 0) + 0):Nat
NAT+> set verbose on
NAT+> parse s 0 + 0 .
((s 0) + 0):Nat
    _+_:Nat
s_:NzNat 0:Zero
    |
    0:Zero
NAT+>
```


## Parsing errors

- CafeOBJ system issues an error message if an equation can not be parsed

CafeOBJ> mod! NAT+ $\{\ldots$
eq (s M) + N = s(M, N)
\}
-- defining module! NAT+
[Error] bad axiom (ignored):
No possible parse for RHS
-- failed to evaluate the form:
a paring error message
axiom declaration(equation):
lhs = ( ( s M ) + N )
rhs $=\mathbf{s}(M, N)$
Cafeobj>

## Debugging specifications

Loading the codes above the point of error and using show and/or parse command to fix the error. "open" command is also effective in debugging modules.

```
NAT+> mod! NAT+DEBUG {
    [Zero NzNat < Nat]
    op 0 : -> Zero
    op s_ : Nat -> NzNat
    op _+_ : Nat Nat -> Nat
    vars M N : Nat
    eq 0 + N = N.
}
- defining module!
    NAT+DEBUG....._.* done.
NAT+> select NAT+DEBUG
NAT+DEBUG>
```

```
NAT+DEBUG> parse s(M, N) .
[Error] no successfull parse
    (s ( M , N ))
("s" "(" "M" "," "N" ")") : SyntaxErr
NAT+DEBUG> parse M .
M : Nat
NAT+DEBUG> parse N .
N : Nat
NAT+DEBUG> parse s(M + N).
(s (M + N)) : NzNat
NAT+DEBUG>
```


## Trace commands

When some reduction in a proof score does not returns "true", the trace commands help us to detect the reason.

NAT+> set trace whole on
NAT+> red +(s(0), s(0))
-- reduce in NAT+ : +(s(0),s(0))
[1]: +(s(0),s(0))
$\cdots s(+(0, s(0)))$
[2]: $s(+(0, s(0)))$
$--->s(s(0))$
s(s(0)): NzNat
( 0.000 sec ...)
NAT+> set trace whole off

```
NAT+> set trace on
NAT+> red +(s(0), s(0))
    -- reduce in NAT+ : +(s(0),s(0))
    1>[1] rule: eq +(s(M:Nat),N:Nat) = s(+(M,N))
        {M:Nat |-> 0, N:Nat |-> s(0) }
1<[1] +(s(0),s(0)) --> s(+(0,s(0)))
1>[2] rule: eq +(0,N:Nat) = N
    {N:Nat l-> s(0) }
1<[2] +(0,s(0)) --> s(0)
s(s(0)) : NzNat
(0.000 sec ...)
NAT+> set trace off
```


## An Example of Modeling/Specifying in CafeOBJ

1. By understanding a problem to be modeled/specified, determine several sorts of objects (entities, data, agents, states) and operations (functions, actions, events) over them for describing the problem
2. Define the meanings/functions of the operations by declaring equations over expressions composed of the operations

## Modeling STACK in CafeOBJ



## Signature of STACK (1)

```
sorts of objects Element Stack
operations empty : returns empty stack without argument
    push : push an element to a stack and returns a new
        stack
    top : get the top element of a stack and returns
                the element
    pop : removes the top element of a stack and
                                    returns the stack
```

```
-- sorts
[ Element Stack ]
-- operations or operators
op empty : -> Stack
op push : Element Stack -> Stack
op pop_ : Stack -> Stack
op top_ : Stack -> Element
```

Signature of STACK (2)


## Terms/expressions generated by the signature

```
Element = { e1, e2, e3, .. }
    U { top S | S E Stack }
```

Stack $=\{$ empty $\}$
$U\{$ push $(E, S) \mid E \in$ Element $\wedge S \in$ Stack \}
U \{ pop S | S E Stack \}

## Examples:

top push(e1,empty) $\in$ Element
pop push(e1,empty) $\in$ Stack
top pop push(e1,empty) $\in$ Element
pop pop push(e1,empty) $\in$ Stack
top push(e2, pop pop push(e1,empty)) $\in$ Element

## Equations

```
-- operations or operators
op empty : -> Stack
op push : Element Stack -> Stack
op pop_ : Stack -> Stack
op top_ : Stack -> Element
-- equations
eq top push(E:Element,S:Stack) = E .
eq pop push(E:Element,S:Stack) = S .
```

```
Examples:
top push(e1,empty) = e1
pop push(e1,empty) = empty
top pop push(e1,empty) = top empty
pop pop push(e1,empty) = pop empty
top push(e2, pop pop push(e1,empty)) = e2
    this is not the intended behavior
```


## Revised signature of STACK (1)



Revised signature of STACK (2)

```
-- sorts and subsorts
[ Element, EmptyStack NonEmptyStack < Stack ]
-- operators
op empty : -> EmptyStack
op push : Element Stack -> NonEmptyStack
op pop_ : NonEmptyStack -> Stack
    -- only applicable to NonEmptyStack
op top_ : NonEmptyStack -> Element
-- only applicable to NonEmptyStack
```


## Terms generated by revised signature

```
Element = { e1, e2, e3, ... }
    U { top S | S E NonEmptyStack }
```

```
EmptyStack = { empty }
NonEmptyStack = { push(E,S) | E E Element ^ S E Stack }
Stack = { pop S | S E NonEmptyStack }
    U EmptyStack U NonEmptyStack
```

Examples:
top push (e1, empty) $\in$ Element
push (e1, empty) $\in$ NonEmptyStack
pop push(e1, empty) $\in$ Stack
top pop push(e1, empty) : not well formed!
pop pop push(e1, empty) : not well formed!
top push(e2, pop pop push(e1, empty))
: not well formed!

Revised Stack -- equations --

```
[ EmptyStack NonEmptyStack < Stack ]
op empty : -> EmptyStack {constr}
op push : Element Stack -> NonEmptyStack {constr}
op pop_ : NonEmptyStack -> Stack
op top_ : NonEmptyStack -> Element
-- equations
eq top push (E:Element, S:Stack) = E .
eq pop push (E:Element, S:Stack) = S .
```

```
Examples:
```

Examples:
top push(e1,empty) = e1
top push(e1,empty) = e1
pop push(e1,empty) = empty
pop push(e1,empty) = empty
top pop push(e1,empty) = (top empty : ?Element)
top pop push(e1,empty) = (top empty : ?Element)
pop pop push(e1,empty) = (pop empty : ?Stack)
pop pop push(e1,empty) = (pop empty : ?Stack)
top push(e2, pop pop push(e1,empty)) =
top push(e2, pop pop push(e1,empty)) =
(top push(e2,pop empty) : ?Element)
(top push(e2,pop empty) : ?Element)
Return value is of Error sort!

```
    Return value is of Error sort!
```


## Revised specification of Stack in CafeOBJ

```
Specification of Stack
mod* ELEMENT { [Element] }
mod! STACK (X :: ELEMENT) {
    [EmptyStack NonEmptyStack < Stack ]
    op empty : -> EmptyStack {constr}
    op push : Element Stack -> NonEmptyStack {constr}
    op pop_ : NonEmptyStack -> Stack
        -- only applicable to NonEmptyStack
    op top_ : NonEmptyStack -> Element
                                -- only applicable to NonEmptyStack
    eq top push (E:Element, S:Stack) = E
    eq pop push (E:Element, S:Stack) = S . }
```

