

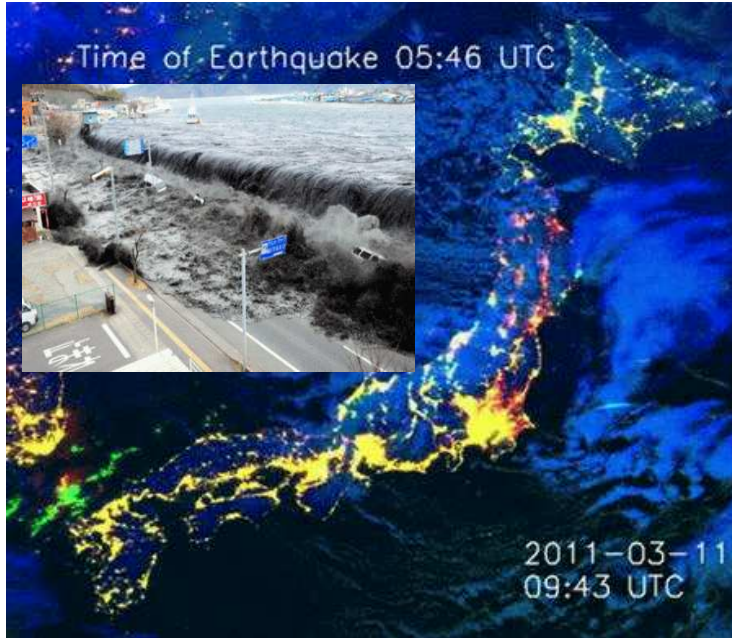
# **-Complex Networks 1.4-**

## **A self-organized design of efficient and strong robust communication networks**

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# Unheard-of earthquake M9.0





# What happened -other disorder



# Further indirect damages

Caused by uncertain, incorrect, and insufficient information

- impossible distribution of drugs, cloths, foods, etc. from temporal storehouses to each evacuation area
- no-accepted military rescues as long as government requires (but already destroyed org.)
- stopping of distant industry supply-chains by lack of parts or the substitutes
- rumors for agricultural and marine products (e.g. radioactive contamination)
- ⋮

# Lifelines interaction

Only experimental analysis of interaction between macroscopic industry domains, **it's too rough sketch !**

from to	water	gas	e-power	comm.	transport	waste
water	-	%	%	%	%	%
⋮		⋮				
comm.	%	%	%	-	%	%
⋮					⋮	
waste	%	%	%	%	%	-

Comm. are particularly important for the regulation and the control of other complex systems: railways, airlines, traffic, energy or food supply, economic, etc.



# Current technologies

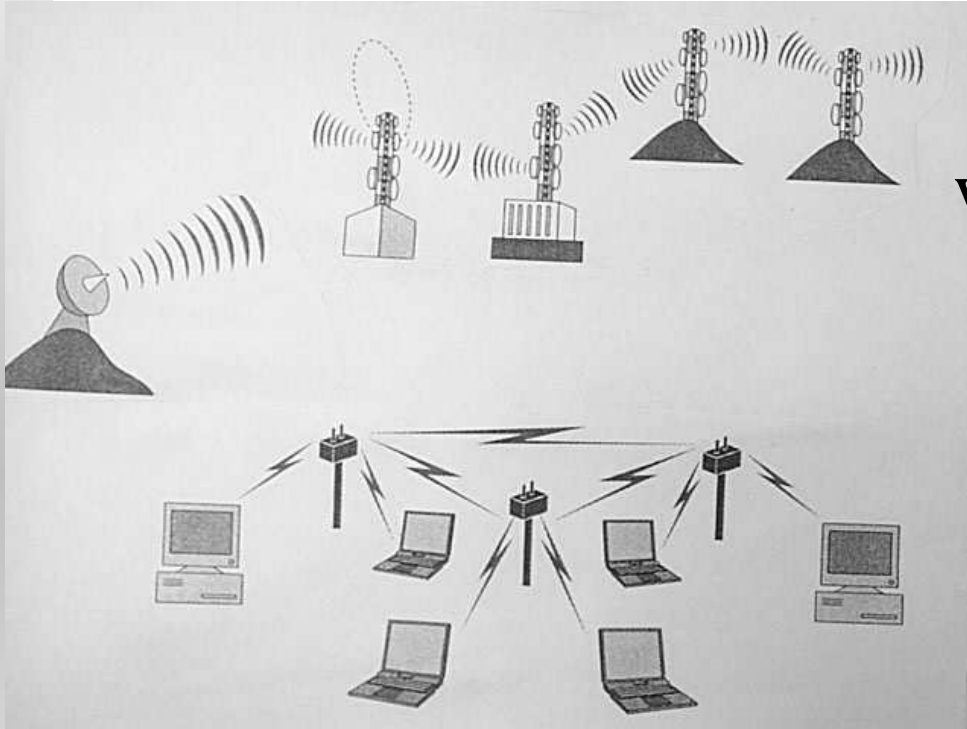


L:Portable satellite equipment R:Movable base-station

We have already some elemental technologies for emergent wireless communication

⇒ Cooperative supports by local communities are very important at social level

# Extendable wireless comm.



with long-range [km] and directional [ $\theta > 30^\circ$ ] beams for wide-area wireless communication at physical device level

However, there are **no systematic ways for network construction**, proper settings of nodes (positions) and linkings are not designed !

# Many real-nets are SF

Common networks structure:  $P(k) \sim k^{-\gamma}$

**Tech.:** airline, Internet(AS, router), WWW, power-grid, P2P, electric circuit

**Social:** acquaintance relationship, actor collaboration, citation, sexual contact, e-mail, language

**Bio.:** neural network(C.elegance), gene network, matabolic pathway, food chain

generated by **the universal mechanism: rich gets richer**  
⇒ It is efficient with short paths but **extremely vulnerable** against hub attacks

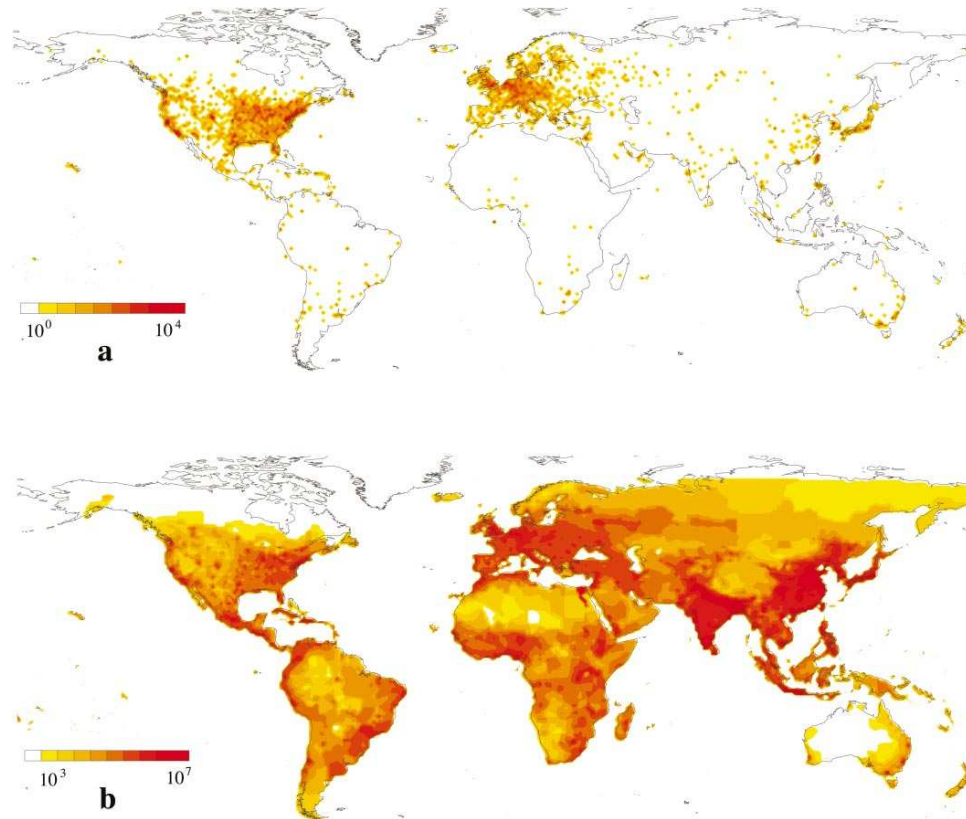
A.L. Barabási et al., Physica A, 272, 1999



# Necessary spatial structure

Nodes are embedded on a space, whose positions are **neither uniformly random nor on a regular lattice**

Density maps of router(top) and population(bottom)

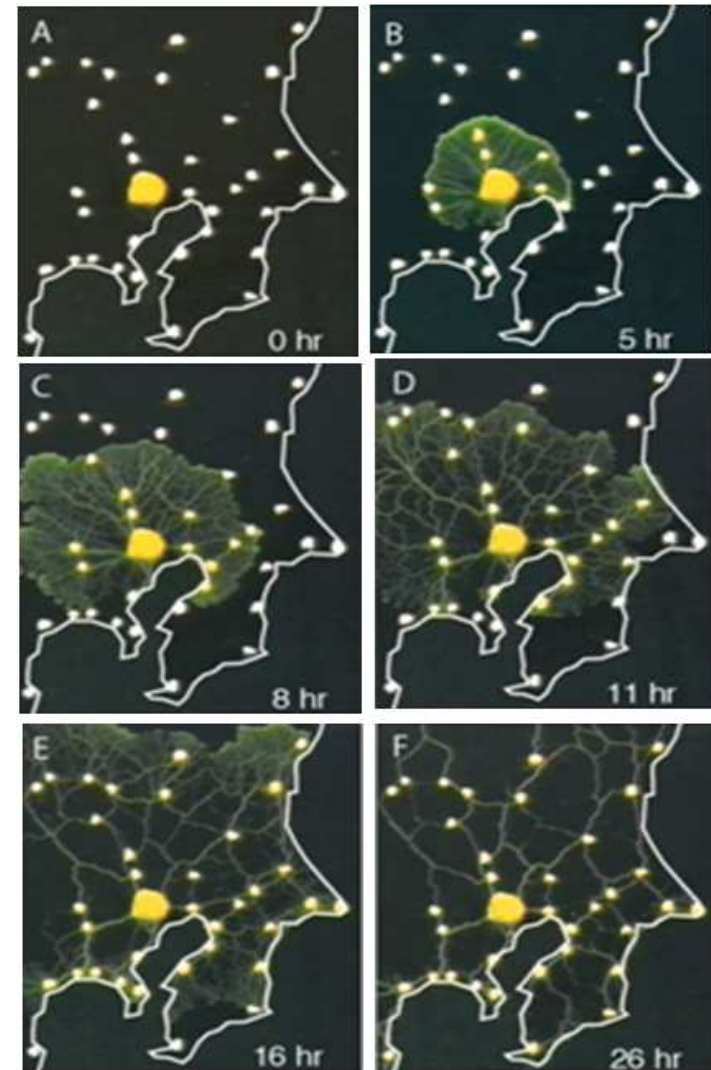


Yook, Jeong, Barabási, PNAS 99(21), 2002

# Remarkable 1

- Slime mold in growing to approach food sources
- Diffusive growth toward chemotaxis in leaf venation and morphogenesis
- Human trail systems

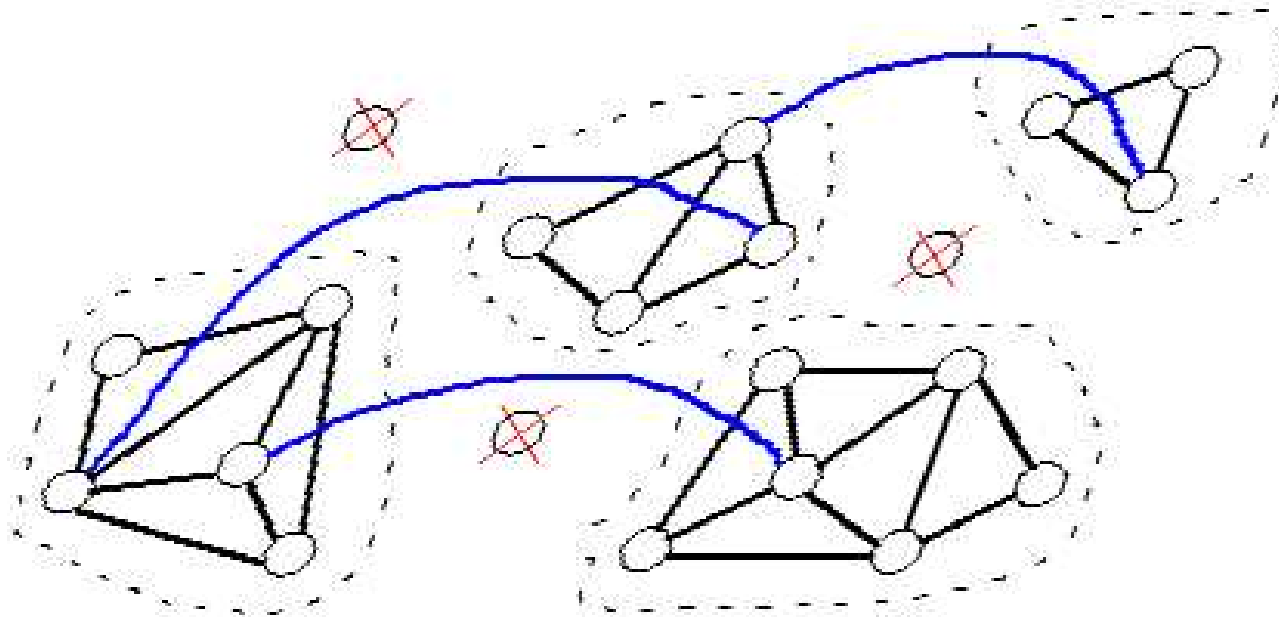
⇒ Selective reinforcement of preferred routes and removal of redundant links as the net. self-organization



A.Tero et al., Science 327, 439, 2010

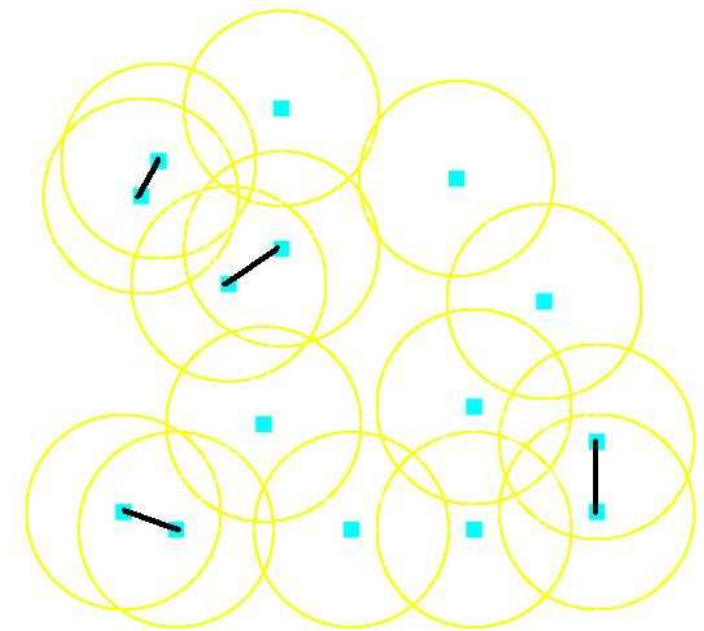
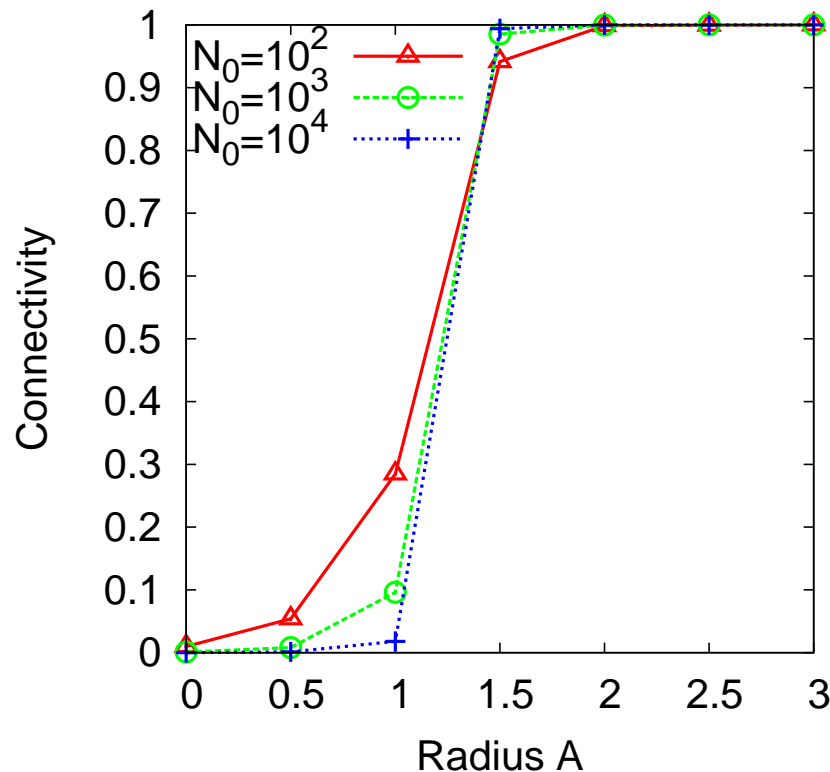
# Remarkable 2

Shortcut effect on robustness in "long-distance relations" and "local or embedded relations"



**Bridge local clusters:** e.g. quick recover in the TOYOTA supply-chain from the 1997 AISIN fire crisis, & rapid growth of Wenzhou people's economical nets.

# Initial configuration



Unit disk graph

Wireless comm. model: UDG on a normalized square

Two nodes  $i$  and  $j$  are connected if  $d_{ij} < A/\sqrt{N_0}$

$\Rightarrow \exists$  Phase transition of the connectivity for the transmission radius  $A$



# Self-organized net. design

We assume that, for a packet transfer, the selection of a node as *source* or *terminal* is **inhomogeneously** proportional to the population in the territory of the nearest access from each mesh block

There are  $R = 0.1N_T$  packets in the network

**Link Survival** If a packet pass a link  $e_{ij}$  on the

(GPS-based) greedy routing,  $w_{ij} \rightarrow w_{ij} + 1$

With prob .  $p_d = 0.01$  for all links,  $w_{ij} \rightarrow w_{ij} - 1$

Until  $T = 3 \times 10^4$  steps, the increasing and the decreasing of  $w_{ij}$  are repeated

When  $w_{ij} = 0$ , **the redundant link  $e_{ij}$  is removed**, and isolated nodes without any links are also removed

# Adding shortcuts

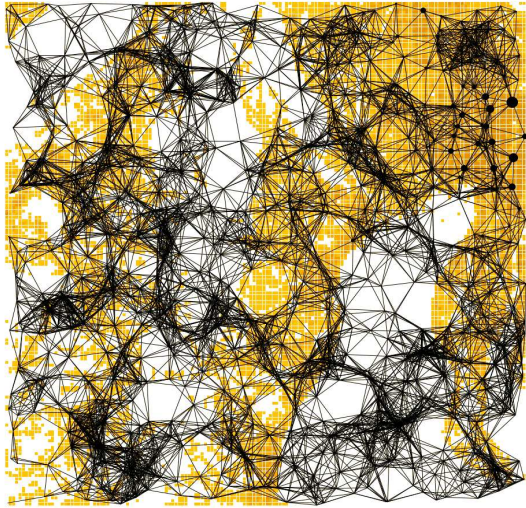
In order to improve the robustness

**Path Reinforcement** After stopping the removal of links at  $T$ , we continue the network generation and the transfer of packets to make 10 or 30% of shortcuts for the total number of survived links in the LS network

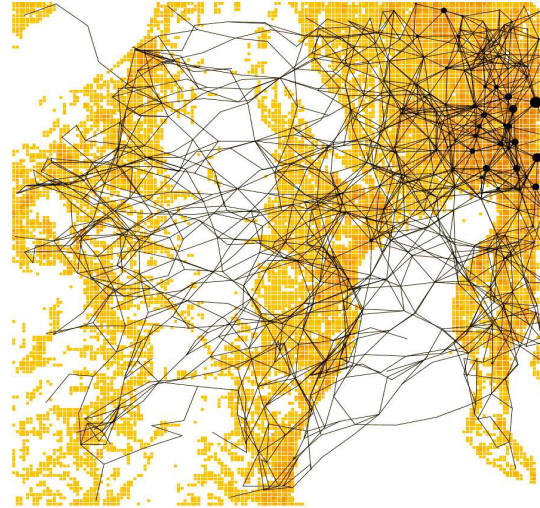
Each shortcut link is added due to **the reinforcement** between the current resident node of a randomly chosen packet and a randomly chosen node from the visited ones **on the path**

**Random Shortcut** On the LS network, we add 10 or 30% of shortcuts between randomly chosen two nodes independent from the positions of packets

# Visualization



UDG



LS

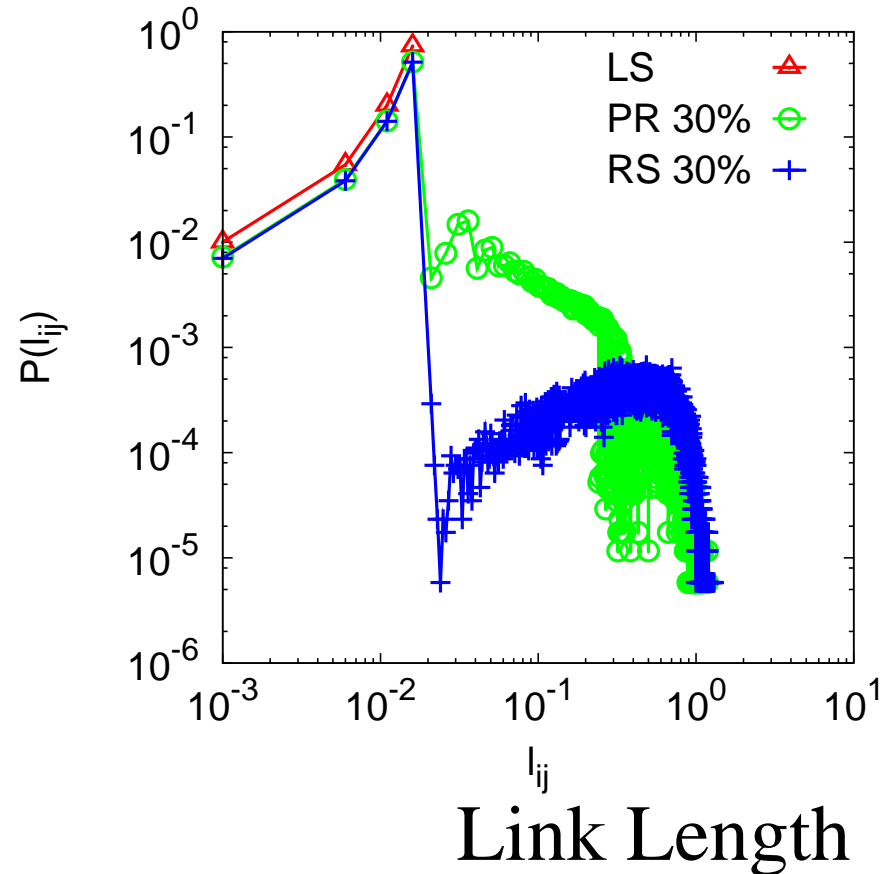
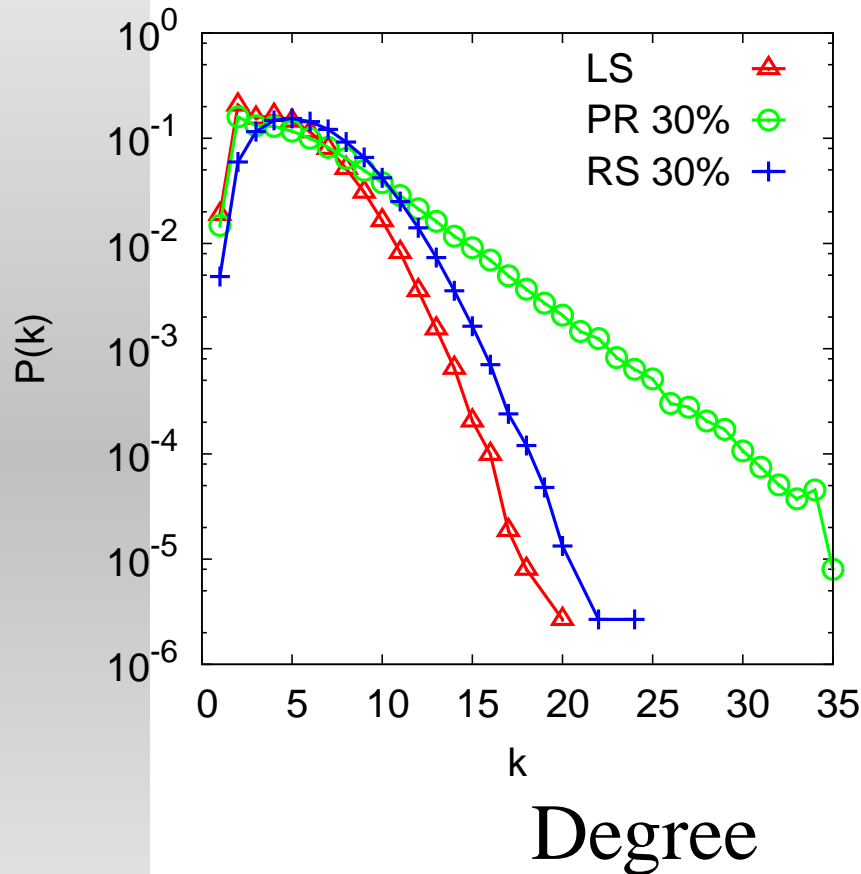


PR10%



RS10%

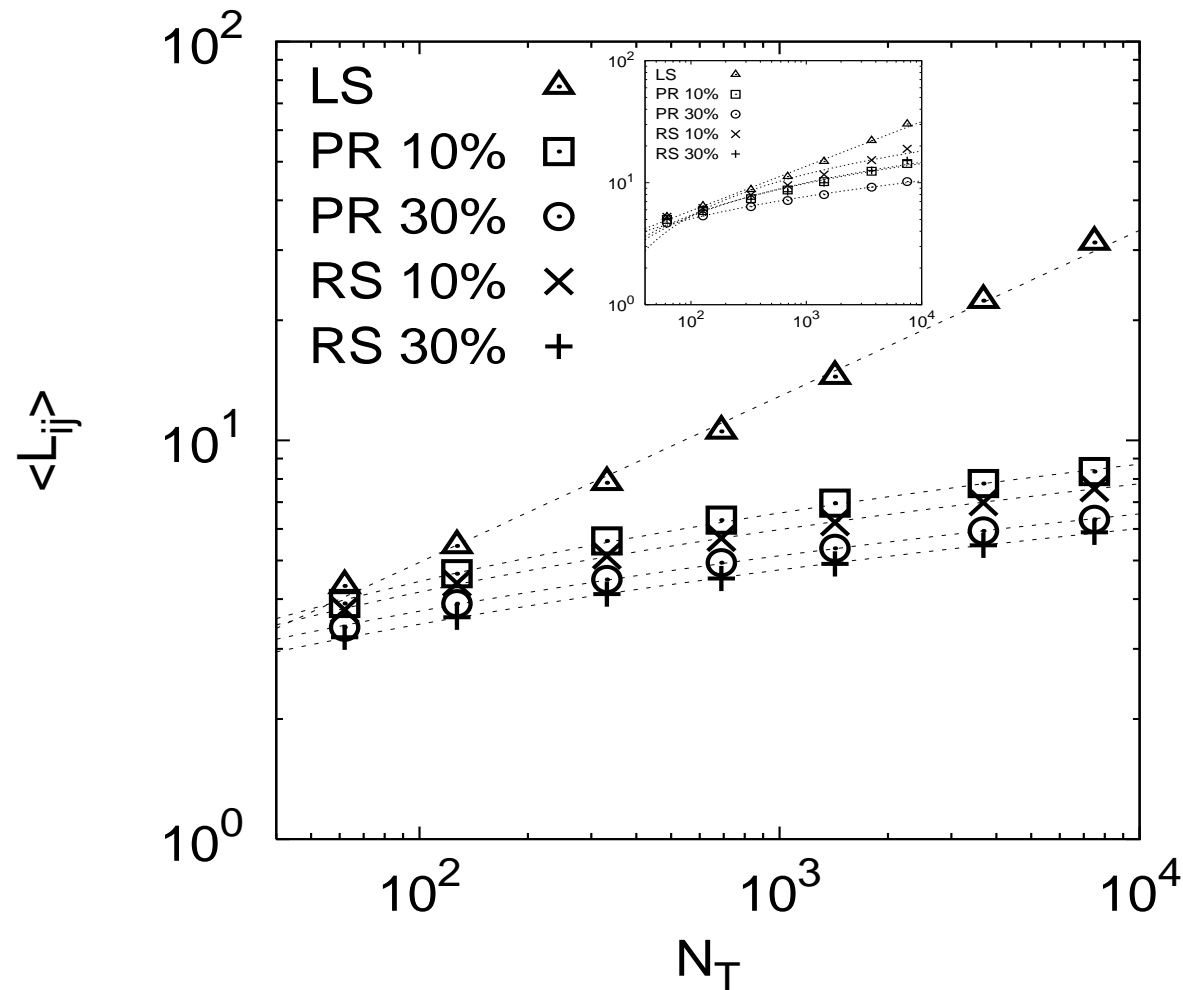
# Structural properties w/o hubs



$\Rightarrow$  Efficiently small degree  $\langle k \rangle = 5 \sim 7$  and short link  $\langle l_{ij} \rangle = 0.01 \sim 0.1$  even with shortcuts at  $N_0 = 10^4$



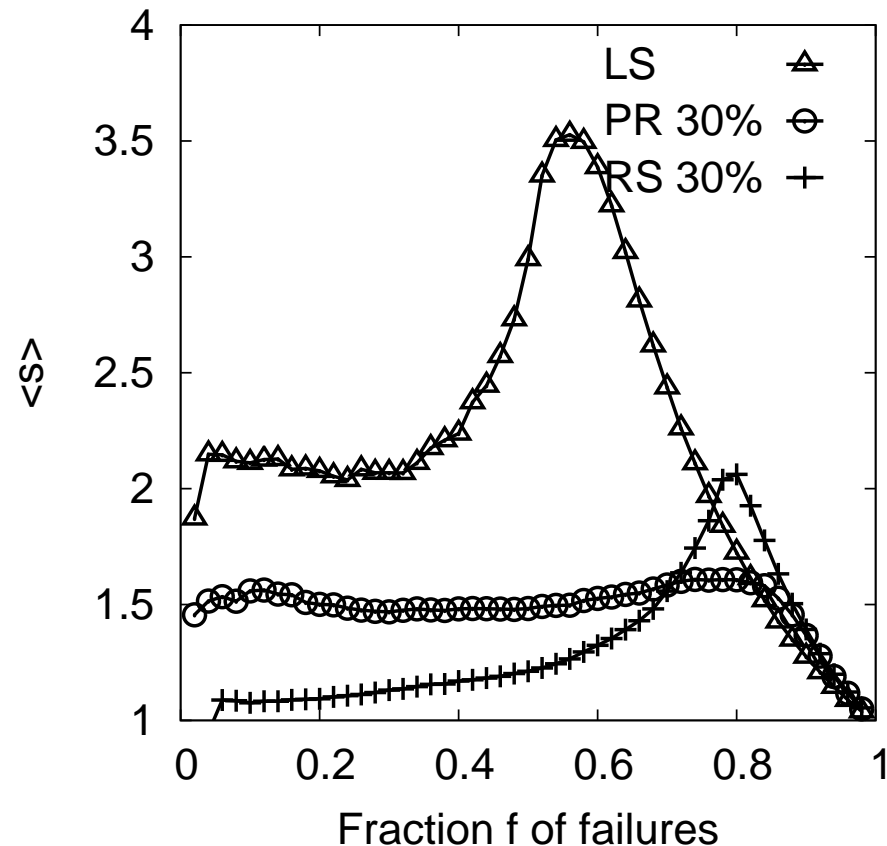
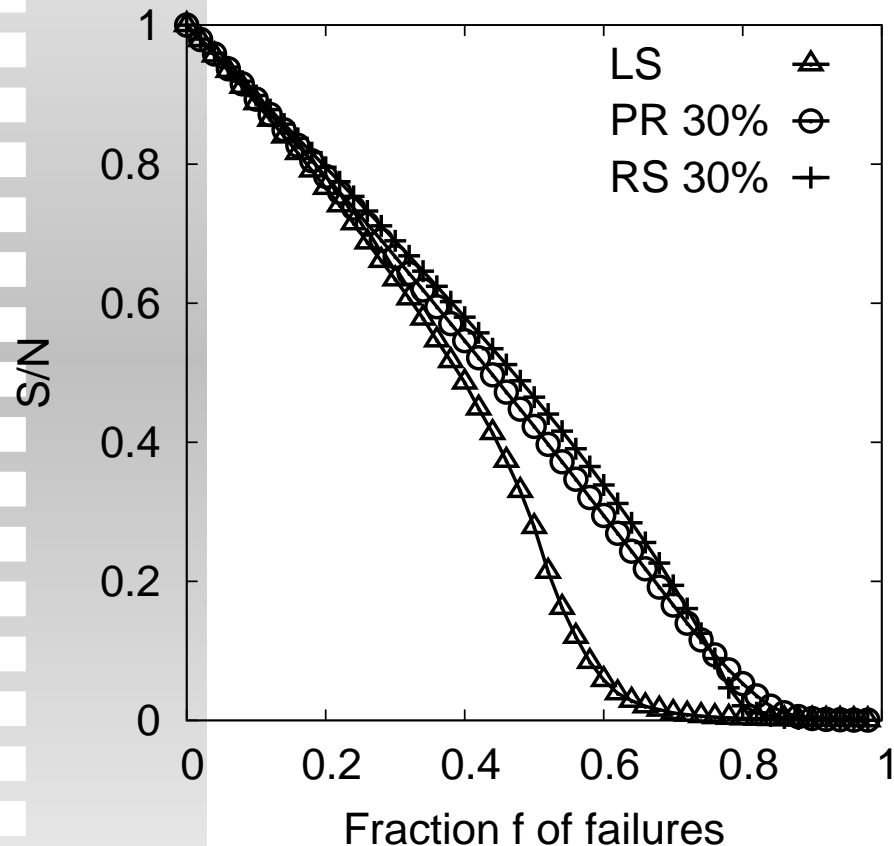
# Ave. path length(hop-count)



⇒ Improved from  $O(\sqrt{N_T})$  in LS to  $O(\log N_T)$  in PR and RS as the small-world effect !

# Strong robustness -failures

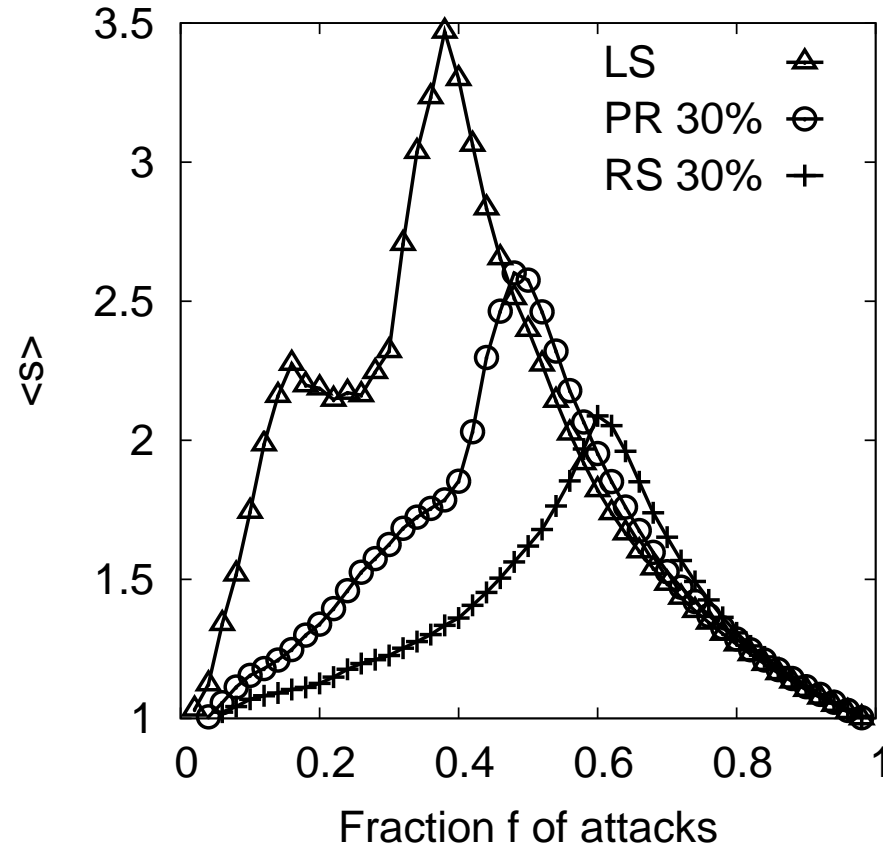
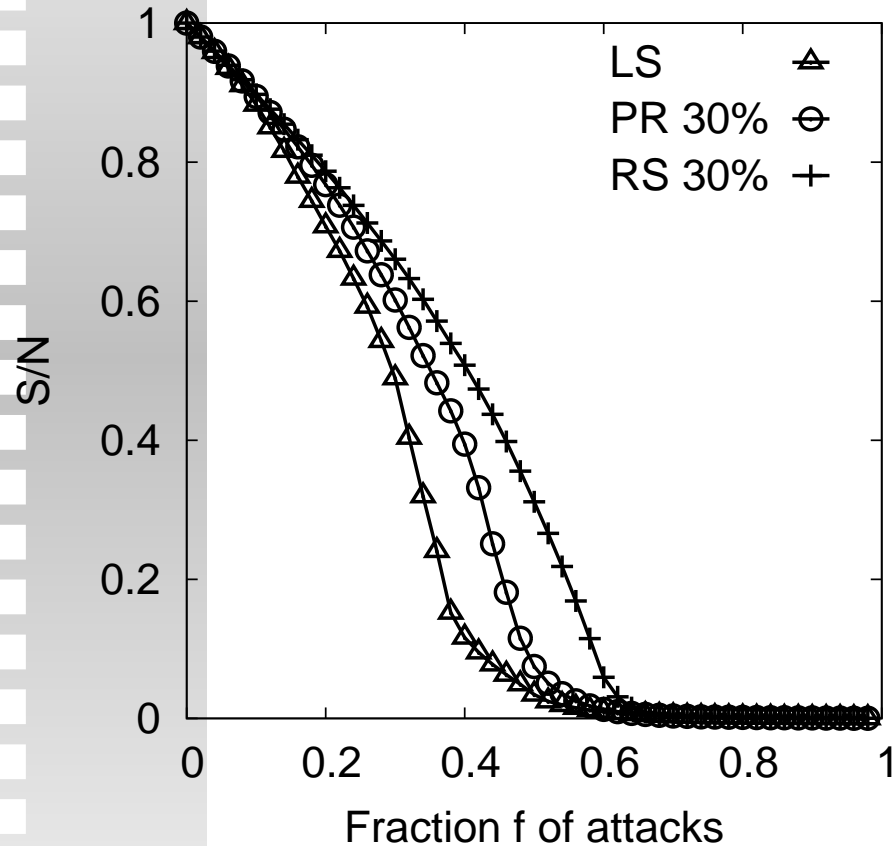
Improved by adding shortcuts



$\Rightarrow f_c$  is increased from **0.6 in LS** to **0.8 in PR and RS**

# Strong robustness -attacks

Improved by adding shortcuts



$\Rightarrow f_c$  is increased from **0.4 in LS** to **0.6 in PR and RS**

# Summary

- We propose self-organized geographical networks by link survival and adding shortcut
- The positions of survived nodes naturally concentrate on the areas of high pop.
- In particular, by adding shortcuts, the average number of hops is improved from  $O(\sqrt{N_T})$  in LS networks to  $O(\log N_T)$  as the small-world effect
- Moreover, for both failures and attacks, the robustness of connectivity becomes stronger

⇒ Thus, our self-organized networks keep the high comm. efficiency in realistic SF nets, but also overcome the vulnerability by the effects of shortcuts



**For your kind attention**



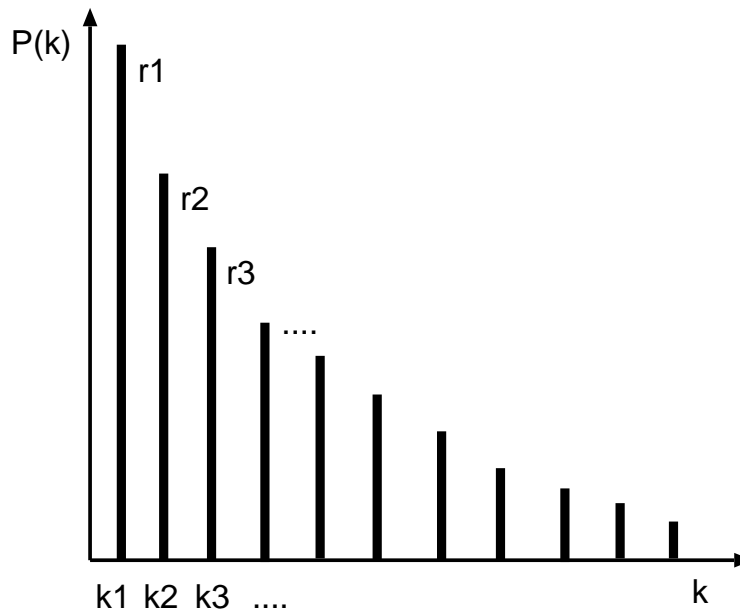
We will never forget your heart warming support!

# A1. Optimal modality

In multimodal nets ( $i = 1, 2, \dots, M$  modalities):

$$k_i \stackrel{\text{def}}{=} k_1 b^{i-1}, \quad r_i \stackrel{\text{def}}{=} r_1 a^{i-1}, \quad a > 1, \quad 0 < b < 1,$$

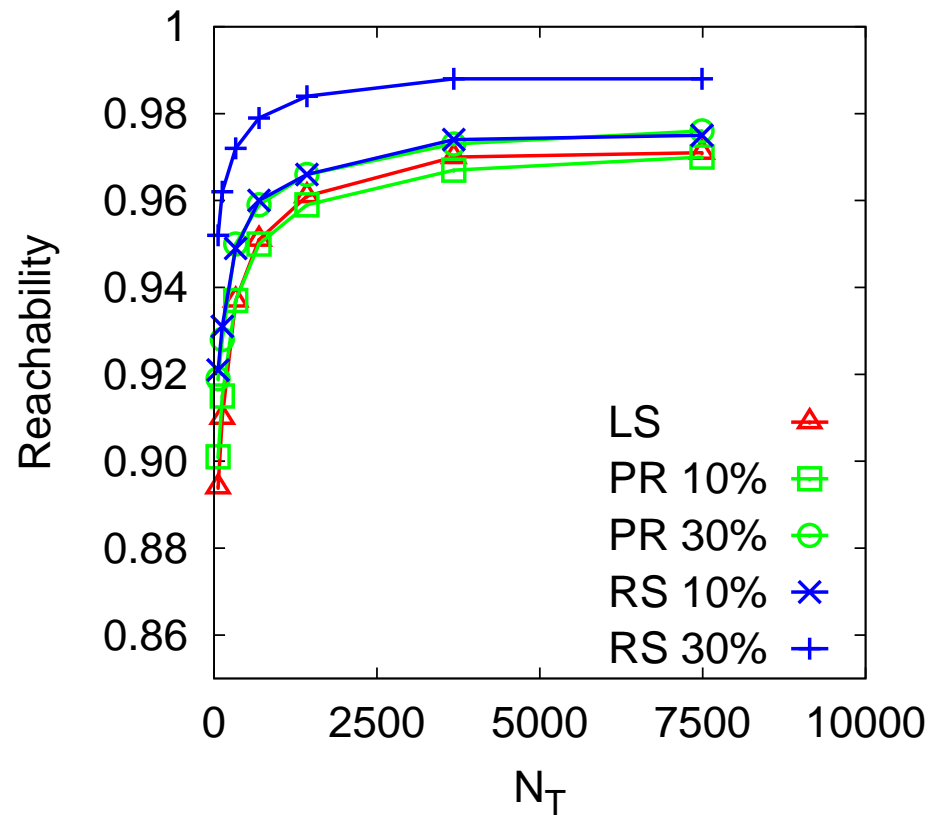
a **bimodal net** with  $k_1$  and  $k_2 = \sqrt{\langle k \rangle N}$  is the best for both failures and attacks, however a **SF net at  $M \rightarrow \infty$  is the worst**



T.Tanizawa, G.Paul, S.Havlin, H.E.Stanley, Phys. Rev. E 74, 2006

# A2. High reachability

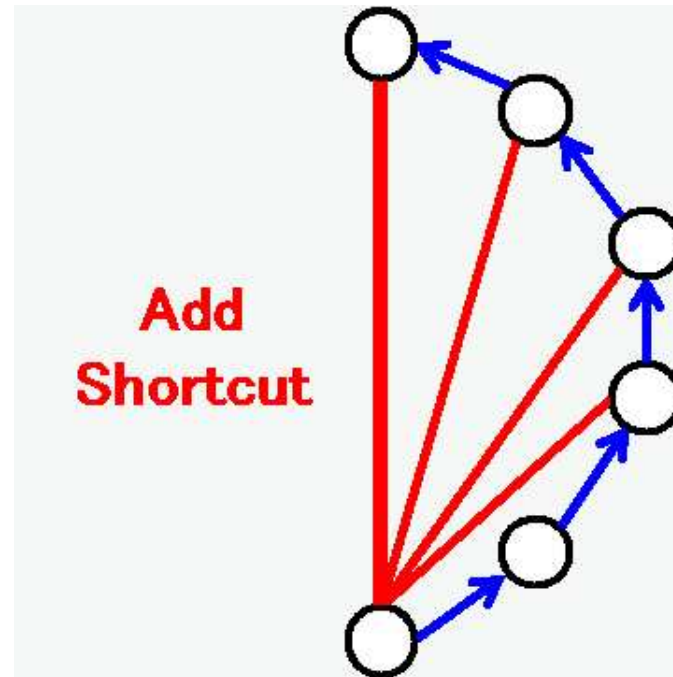
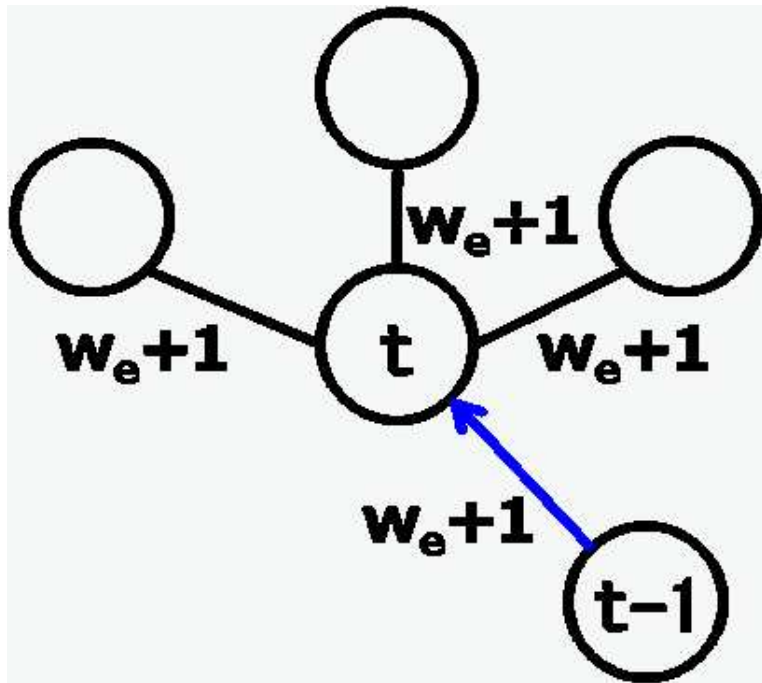
for the greedy routing with self-avoiding



UDG	100	200	500	1000	2000	5000	10000
$N_T$	61.94	127.0	331.26	688.94	1425.4	3679.98	7489.92

# A3. Coupled models

with network construction and flow dynamics



(Left) phase transition by the **hub emergence**

S.-W. Kim, J.D. Noh, PRE 80, 026119, 2009

(Right) **quasi-complete graph** on 1D, SF net on 2D

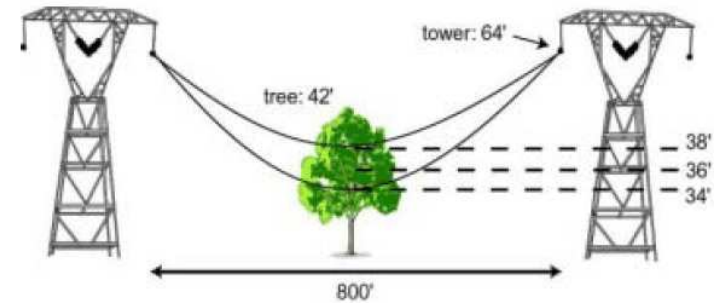
N.Ikeda, Physica A 379, 701, 2007

# A4. Cascading failure

If the e-power or the flow exceeds the node or link capacity

∃ same mechanism in:

- crisis of power-grid from initial disconnections to wide area blackout
- congestion in traffic and Internet
- ∴



NERC “August 14 2003  
Blackout”



# A5. Trends of mega-city hazards

- Mixes of natural, technological, and social hazards are increasingly common
- Risks are changing slowly
- Loci of hazards are shifting markedly
- Differentially vulnerable groups are becoming polarized and segregated
- Public support for hazard-management initiatives may be faltering
- Overlaps among hazard and urbanization issues offer opportunities for managerial intervention

J.K.Michell ed., *Crucibles of hazard: Mega-cities and disasters in transition*, Chap.13, United Nations University Press, 1999